# Analytical Geometry and Enriched Uranium Solutions in SCALE: Two H-Canyon Studies 

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## Overview

- Part 1: Simple Model and Complex Physics Behavior
-HEU Solution stored in sloped bottom tanks
-Projected Areal Density
- Function relationship
- Part 2: Complex Model and Simple Behavior
-Section 6 Hot of H-Canyon
- Dissolver Operations
-Do dissolvers see each other?


## Part 1



## Motivation for Inquiry

- Investigation was made to establish a mass limit for H Canyon vessels based on areal density
-Most vessels have sloped bottoms
-In some cases, areal density based mass limits were still usable
- Is there a functional relationship between slope of the tank and the use of an areal density based mass?
-What does areal density mean in light of sloped tanks?


## Background

- Areal density projects the mass of a 3-D system onto a single plane
-Physically comparable to infinite slab of certain thickness
-Well-understood, experimental basis, easily modeled in computational codes
- Assumes that the surface of projection is orthonormal to the remaining dimensions of the system
-Most commonly project vertical axis onto $x$-y plane to reference material staged on a floor, tank, table, etc.
- In sloped bottom tanks, the bottom plane is not orthonormal to the remaining dimensions!
-Flat is not always economic, convenient, available, or safe from a chemical or processing hazard aspect


## Background

- Is there a relationship between slope, area, and what may be called a projected areal density (PAD) where the plane of projection is not orthonormal to the other dimensions?
- Remember: Areal density is a mathematical construct
-Modifying the construct in this work, the projection surface is sloped $\rightarrow$ PAD


## Analytical Approach

- Computational modeling performed in KENO-VI of SCALE 6.1
-Validated internally for use in HEU aqueous systems
- Calculations parallel data available in LA-10860
-pure ${ }^{235} \mathrm{UO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$
-no excess nitric acid (removes poisoning effect)
-full reflection modeled by 60 cm of water in all directions
-reflective boundary conditions.
- Used the KENO macrobody of a rotated wedge to simulate sloping of the bottom head.


## Analytical Approach

- Tank Radii
-51.4, 70.5, 121.0, and 150.5 cm
- Slopes
$-0,3.15,5,7.5,10,15 \%$
- For fixed slope and radius, vary the solution height from 6.35 cm to 300 cm
- Critical concentration search
-within $1.000+/-0.001$
-statistical uncertainty less than 0.001
 $\Delta k$
- Can back calculate fissile mass, H/fissile, etc.


## Analytical Approach

- PAD presented here is defined as projected onto the solution surface
-Data could easily be renormalized to project onto the sloped tank bottom.
- Similar results are obtained from this approach
- When solution height is less than depth of the "shallow end", solution takes on shape of a truncated wedge. -No reason limiting PAD would not occur in these conditions



## Methodology - Partially Filled Sloped Bottom

- Volume requires numerical integration
-Integrate area over height
- If deep end depth is $h$ and fraction slope of the tank is $I$, then volume of the solution is:

$$
\begin{aligned}
& V_{S} \\
& =\int_{0}^{h}\left\{\frac { - r ^ { 2 } } { 2 } \left[\left(2 \operatorname{acos}\left(1-\frac{2 r-h^{\prime} / l}{r}\right)\right)\right.\right. \\
& \left.\left.-\sin \left(2 \operatorname{acos}\left(1-\frac{2 r-h^{\prime} / l}{r}\right)\right)\right]+\left[\pi r^{2}\right]\right\} d h^{\prime}
\end{aligned}
$$



- Line $a$ is the line solution makes with the shallow end of the tank


## Methodology - Partially Filled Sloped Bottom

- As is the surface area we are interested in
- Area of the yellow segment is

$$
\frac{r^{2}}{2}(\theta-\sin \theta)
$$

- Knowing $2 \mathrm{r}=\mathrm{Q}+\mathrm{L}$
- $L$ is determined by depth of solution and
 fractional slope
- At a solution depth of $\mathrm{h}^{\prime} \theta=2 \operatorname{acos}\left(1-\frac{2 r-h^{\prime} / l}{r}\right)$


## Results - PAD

- For each radius and slope, determined the minimum PAD that would result in a critical configuration
-As would be done with areal density on flat bottoms tanks -Critical heights are measured from the "deep end" of the solution, i.e. the point that would be tangent to the low end tank wall


## Results - PAD

## PAD for $\mathbf{1 2 1 . 0}$ cm Radius Tank



## Results - PAD

- Minimum PAD ( $\mathrm{g} \mathrm{U}-235 / \mathrm{cm}^{2}$ ) for various conditions

| Slope | 51.4 <br> cm radius | 70.5 <br> cm radius | 121.0 <br> cm radius | 1.50 .5 <br> cm radius |
| :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 0.4919 | 0.4669 | 0.4456 | 0.4414 |
| $3.15 \%$ | 0.4904 | 0.4588 | 0.4022 | 0.3677 |
| $5 \%$ | 0.4868 | 0.4476 | 0.3507 | 0.2845 |
| $7.5 \%$ | 0.4781 | 0.4219 | 0.2886 | 0.2651 |
| $10 \%$ | 0.4685 | 0.3887 | 0.2753 | 0.2627 |
| $1.5 \%$ | 0.4305 | 0.3335 | 0.2803 | 0.2713 |

- Can be translated into more physical quantities
- Mass (g): 3580 to 31400 depending on tank size
-Concentration (g U-235/L): 25.5 to 44.0, average 31.6
- H/U-235: 575 to 1015, average 825


## Results - Overall Behavior Fitted

Behavior of PAD in Sloped Tanks


## Results - Coefficient Fitting

Behavior of Fitting Coefficients


$$
-\mathrm{x}^{\wedge} 2-\mathrm{x}-\operatorname{int}
$$

## Results - Function Fit

- PAD $=\left(6.199 * 10^{-8}\right) \mathrm{s}^{2} \mathrm{r}^{2}+\left(8.786^{*} 10^{-7}\right) \mathrm{sr}^{2}+\left(2.126^{*} 10^{-6}\right) \mathrm{r}^{2}+$ $\left(9.071^{*} 10^{-6}\right) s^{2} r-\left(5.674 * 10^{-4}\right) \mathrm{sr}-\left(8.537^{*} 10^{-4}\right) \mathrm{r}-$
$\left(1.086^{*} 10^{-3}\right) s^{2}+\left(2.919^{*} 10^{-2}\right) s+\left(5.262^{*} 10^{-1}\right)$
- Fit Predicted PAD Percent Different with Calculated:

| Slope | 51.4 <br> cm radius | 70.5 <br> cm radius | 121.0 <br> cm radius | 150.5 <br> cm <br> radius |
| :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | -0.81 | 2.08 | 1.89 | 1.02 |
| $3.15 \%$ | 0.06 | -0.85 | -5.67 | -5.30 |
| $5 \%$ | 0.29 | -1.50 | -1.91 | 7.70 |
| $7.5 \%$ | 0.36 | -0.33 | 6.13 | 1.21 |
| $10 \%$ | -0.60 | 2.47 | 1.71 | -4.38 |
| $15 \%$ | -2.35 | 4.59 | -6.60 | 3.24 |

## Conclusions - Part 1

- PAD relationship found to be approximately parabolic in radius and slope
- Could be used to adjust down the ANS 8.1 single parameter areal density by this trend (function or data)
-apply lower PAD to the cross-sectional area of the tank in question
-some small additional margin
- Could select the lowest PAD and apply that value
-Provided radius and slope are bounded by the available data


## Part 2



## Section 6 Hot - Complex Model for Simple Question

- Canyon is divided into warm and hot sides based on intensity of radiation from the processes
- Divided into 18 sections
- Section 6 Hot contains dissolution operations
- Primary objective to generate highly detailed model of Section 6 Hot
-Beyond single vessel, homogenous fuel simplified models
- Do the vessels communicate neutronically?



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## Results Part 2 - As Modeled

- 6.1D k-effective: 0.6628
- 6.2R/F k-effective: 0.0000 (No fissile assumed)
- Sump k-effective: 0.2673
-6.3D k-effective: 0.4167
- 6.4D k-effective: 0.7587
- 6 Hot k-effective: 0.7592
- Communication: No
-As expected


## Questions

## Additional Slides

## Results - Overall Behavior - Wedge Limited

- Height at which Solution Breaks Plane of Shallow End

| Slope | 51.4 <br> cm <br> radius | 70.5 <br> cm radius | 121.0 <br> cm radius | 150.5 <br> cm radius |
| :---: | :---: | :---: | :---: | :---: |
| $3.15 \%$ | 3.24 | 4.44 | 7.62 | 9.48 |
| $5 \%$ | 5.14 | 7.05 | 12.10 | 15.05 |
| $7.5 \%$ | 7.72 | 10.57 | 18.15 | 22.57 |
| $10 \%$ | 10.29 | 14.10 | 24.19 | 30.10 |
| $15 \%$ | 15.43 | 21.15 | 36.29 | 45.15 |

- Highlighted cases are where minimum PAD occurred in truncated wedge shape


## Results - PAD



## Results - PAD

## PAD for 70.5 cm Radius Tank



## Results - PAD



## Results - Overall Behavior

Behavior of PAD in Sloped Tanks


- Fitted PAD

| Slope | 51.4 <br> cm radius | 70.5 <br> cm radius | 121.0 <br> cm radius | 150.5 <br> cm radius |
| :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 0.4879 | 0.4766 | 0.4540 | 0.4459 |
| $3.15 \%$ | 0.4907 | 0.4549 | 0.3794 | 0.3482 |
| $5 \%$ | 0.4882 | 0.4409 | 0.3440 | 0.3064 |
| $7.5 \%$ | 0.4798 | 0.4205 | 0.3063 | 0.2683 |
| $10 \%$ | 0.4657 | 0.3983 | 0.2800 | 0.2512 |
| $15 \%$ | 0.4204 | 0.3488 | 0.2618 | 0.2801 |

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- Height at which Solution Breaks Plane of Shallow End

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| $10 \%$ | 10.29 | 14.10 | 24.19 | 30.10 |
| $15 \%$ | 15.43 | 21.15 | 36.29 | 45.15 |

 wedge shape



## PAD for 51.4 cm Tank




| Slope | cm radius | cm radius | cm radius | cm radius |
| :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 0.4879 | 0.4766 | 0.4540 | 0.4459 |
| $3.15 \%$ | 0.4907 | 0.4549 | 0.3794 | 0.3482 |
| $5 \%$ | 0.4882 | 0.4409 | 0.3440 | 0.3064 |
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